



Study the Space –Time Variations of Indus River Flow Propagation

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Authors' contributions

This work was carried out in collaboration between both authors. Author SAH designed the study, performed the statistical analysis, wrote the protocol, managed the literature and wrote the first draft of the manuscript. Author MRKA managed the analyses of the study and final editing of the manuscript. Both authors read and approved the final manuscript.

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ABSTRACT

River flow is the most important geophysical process of the earth and its ecosystem. Being very unpredictable in nature, at several times its ensemble flow propagation along the network becomes hazardous flood, that causes enormous damage and loss. Pakistan is an agricultural country with one of the world's largest Indus River system. The system undergoes great climatic, strong seasonal and inter-annual variability dominated by both monsoon and snow-glacier dynamics of the Himalayan and Karakoram regions. A better understanding of the variability may provide insight into the problems associated with unpredictable variations in river flow and their propagation. This paper is an attempt to enhance the current knowledge of the Indus River flow dynamics along the network. For this purpose linear and nonlinear methods of propagation analysis of the mean 10 daily river flow (TDF) are utilised. The linear and nonlinear schemes employ cross-correlation and the normalized average of cross-mutual information (MI) method respectively. The overall dominant mechanism of the system shows a linear behaviour, however, some stations demonstrate nonlinear propagation in the network. The results of these analyses may also provide the viability to study the behaviour of regional and global climatic parameters related to the type of information propagated.

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1. INTRODUCTION

Pakistan is an agriculturally dominant country demanding full utilization of its water resources based on one of the world's largest Indus River System (IRS) in the world. This river system is nourished by melting of snow and glaciers in most parts of the year, orographic rainfall, monsoon in summer (June -to- September) [1,2] and western monsoon in winter-spring (February-to- May) seasons [3]. The increase in water level begins in April and in June-July it rises to the maximum level. On several occasions, it produces heavy flooding; not only due to rainfall and melting of glacier snouts and/or ice bridges, but also due to the temperature triggers disastrous avalanches snowstorm in the glacier areas. Thus, the system is always threatened by severe catastrophic floods, especially, during the monsoon season. The flooding situation arrives every year, but on some occasions it becomes disastrous, causing loss of lives and destruction of property, agriculture, buildings, watercourses and etc. Moreover, the excessive water of flood is usually drained out to the sea due to poor water control-arrangements.

The impact of local climate analysis on the IRS network is significantly dominating on the river flow system [4,5]. It may show some considerable nonlinear behaviour of seasonality and stochasticity in the Indus River flow [6,7,8,9]. To investigate the influential role of the regional climatic parameters on the river flows along the IRS network, this paper introduces linear and nonlinear methods of river flow propagation analysis. In this respect, river flow data from Kotri (considering as the lowest reference station) with all six upstream stations (Sukkur, Guddu, Taunsa, Chashma, Kalabagh and Tarbela,) mean 10 daily flow (TDF) along the Indus River (Fig. 1) is analysed. This procedure is also repeated for Sukkur and Guddu (second and third last stations) as reference stations. The linear method evaluates cross-correlation of two data arrays for different lag values, where, cross-correlation is a simple Pearson's correlation technique. The nonlinear estimation considers normalized average of cross-mutual information (MI) method between the two data series. The MI among the two data series is a way to extract the nonlinear information (correlation) between them [10,11,12,13,14].

This paper investigates the existence of linear and nonlinear propagation behaviour in the TDF along the Indus River. The overall dominance of the TDF propagation along the Indus River is linear however, some stations demonstrate nonlinear behaviour. The results of this study will also lay the foundations for some of our future studies related to the behaviour of regional and global climatic parameters and the type of information they propagate.

2. MATERIALS AND METHODS

This section analyses the linear and nonlinear variations in the Indus River flow from each of the lower three stations (Kotri, Sukkur, and Guddu) to all their upstream stations. The linear analysis considers cross-correlation method and nonlinear scheme utilised mutual information technique [6]. These techniques applied to TDF data series of two different stations river flows. The linear method evaluates cross-correlation of two data arrays at different lag values where, cross-correlation is a simple Pearson's correlation techniques. To find the cross mutual information (MI; relative nonlinear information) between two different data series, various techniques available for calculating MI are discussed in details in [15]. One of those techniques is the equal probable binning method (joint probability calculation) that will be used to estimate MI. The mutual information method measures the amount of information of one data series contained about the other. The MI is computed as

$$MI(K, N) = \sum_{k, n} P_{KN}(k, n) \ln \frac{P_{KN}(k, n)}{P_K(k) P_N(n)}$$

Where K and N are the two different data series (this paper considers two different locations, river flow data series) with joint probability function $P_{KN}(k, n)$ and marginal probability functions $P_K(k)$ and $P_N(n)$. Usually river flow distributions functions are negatively skewed, high frequency of low values and low frequency of higher values. The MI is also defined as the relative entropy between the joint and product marginal distributions [16,17,18].

2.1 Linear Analysis of TDF

To develop the linear method scheme Kotri is considered as reference station for evaluation of

cross-correlation with all their upstream stations TDF data. Fig. 1a (height of different markers) shows the estimated cross-correlation values between Kotri with self and all their upstream station's TDF from lag = -4 to lag = 4. Beyond lag = ± 4 the space time variation in the cross-correlation values make no significant change. These values are now connected by dashed lines in such a way that each curve represents the linear relation from Kotri to Kotri (autocorrelation) and with all their upstream station. The curves depict attenuation and shifting behaviour because all upstream stations have some (unequal) distances from Kotri. To represent their trend, draw a thick black line that starts from Kotri-Kotri (peak cross-correlation value = 1) to the appropriate maximum of the lagged cross-correlation value curve of the Kotri-to-other stations. As we know that cross-correlation values represent the linear relation between the two data series, so this thick line can be considered as the propagation of linear information of the river flow. It means that the linear information is at maximum = 1 at Kotri-Kotri cross-correlation value (at lag = 0 or autocorrelation at lag = 0) and it gradually decreases for Kotri-to other upstream station cross-correlation values along the Indus River, because of the water contribution from other resources and as well as their agricultural and domestic supplies, seepage, and evaporation, all are unevenly distributed. To see this decreasing trend more prominently Fig. 1a transformed into the space-time diagram (Fig. 2), for each lag value. Moreover, to represent the above

discussed propagation of linear information behaviour draw a thick black line starting from the maximum value (at Kotri-Kotri) follow appropriate maximum lag cross-correlation values of Kotri-to other stations. This thick line exhibits a decreasing linear trend (Fig. 2) and is called as a liner information propagation roll-off (LR) curve. It is drawn by curve drawing facility of the Microsoft drawing software [19]. This LR curve is based on cross-correlation vales obtained from TDF data series, they may also approximate the cross-correlation curves (at the appropriate higher lags values) of the high resolution data series like the daily, hourly or at every minute. Now repeat the same procedure of drawing LR curve from the other two reference stations of Sukkur and Guddu (Figs. 2b & 2c). These LR curves approximate as a part of the LR curve of Fig. 2a.

Reviewing all cross-correlation curves in Fig. 2a it appears that around Taunsa station all of these become closer to each other while approaching to the Kalabagh station and beyond it they all spread away. This major change in cross-correlation curves are because of the Kabul River meet Indus main stream between Tarbela and Kalabagh station. The Kabul River starts seasonal rising one month earlier than the Indus River. However, after Taunsa station in the downstream there is no major river meeting the Indus main stream. Moreover, between Taunsa and Kalabagh the cross-correlation values have a different structure of variation not only because of the natural linear information roll-off behaviour

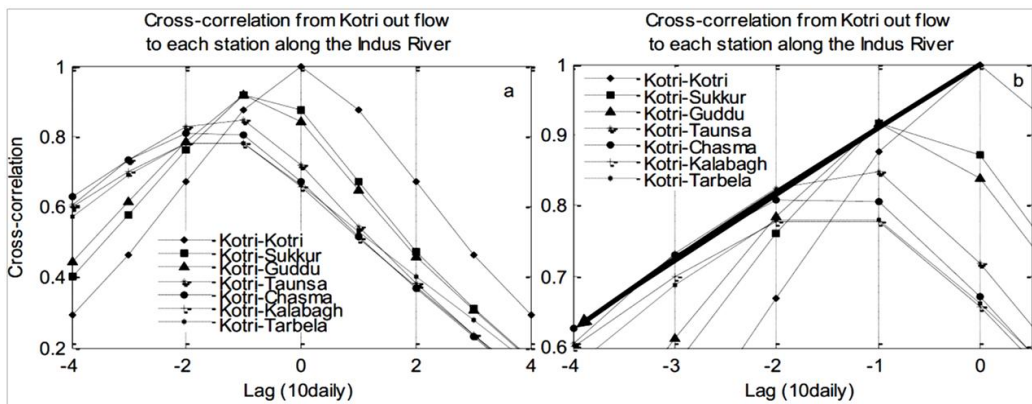


Fig. 1. Linear information propagation in TDF data series using cross-correlation analysis between Kotri with itself and with all its upstream station's along Indus river, vs lag values (a) the appropriate stations cross-correlation values are connected with dashed lines (cross-correlation curves), and (b) the cross-correlation curves roll off (LR) behaviour, shows with thick black line, starts from Kotri-Kotri at lag = 0 follow appropriate maximums of the cross-correlation values of Kotri-to-Sukkur at lag = -1, Kotri-to-Taunsa at lag = -2 and end at Kotri-to-Chashma at lag = -1

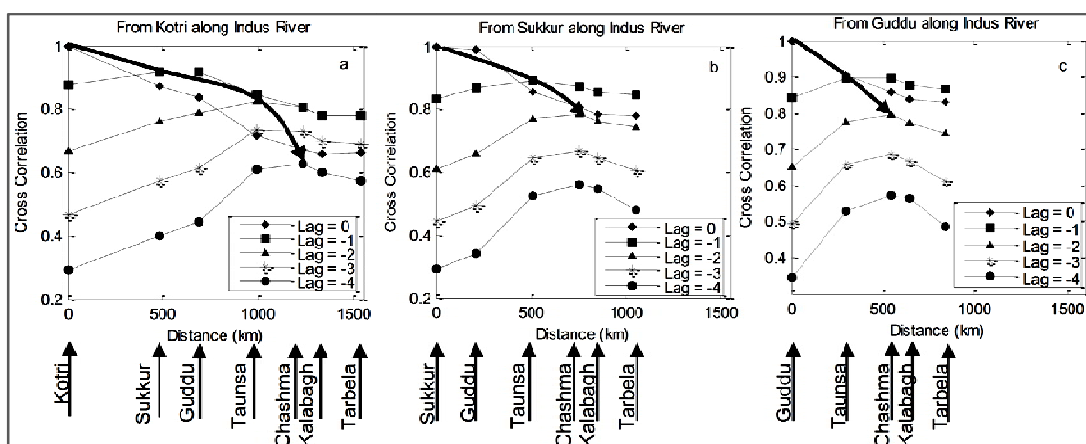


Fig. 2. The LR curve (thick line) is prominently viewed, start from Kotri, follow maximum cross-correlation curves value (thin line) at proceeding lag of space-time cross-correlation analysis (method developed by space-time transformation of Fig. 1), from lower three stations (a) Kotri, (b) Sukkur, and (c) Guddu with itself and with all its upstream station's along Indus river

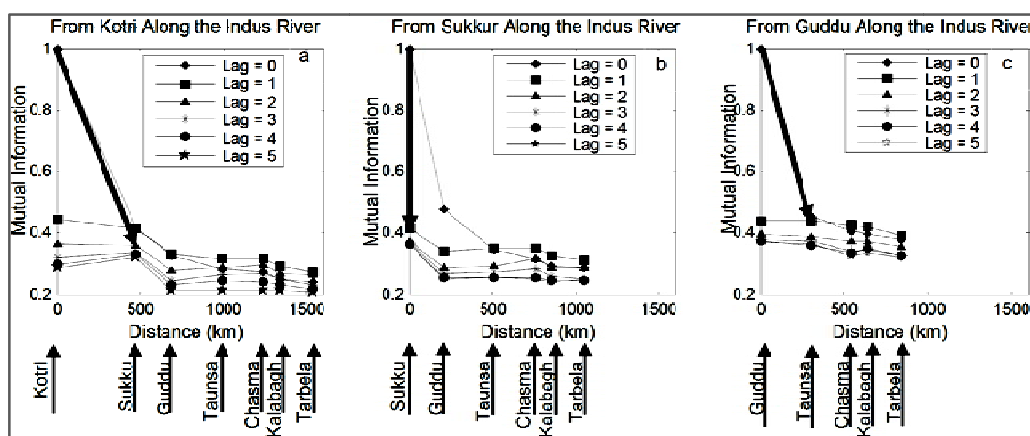


Fig. 3. The NR curve (Thick line) behaviour acquired from space-time MI analysis (obtained as the same procedure developed in Figs. 1 & 2), from lower three stations (a) Kotri, (b) Sukkur, and (c) Guddu with itself and with all its upstream station's along Indus river

but also because of the fact that these stations are much closer to each other as compared to the other downstream stations.

The LR curve with reference to the Kotri station along the Indus River (Fig. 2a) have their highest (maximum) value at Kotri station and gradually roll-off their values (following next lag maximum CC values) in upper stations and completely drop off at Chashma. This LR curve shows that the TDF of the lower four stations are very well linearly correlated. The space-time LR curves in Figs. 2b & 2c have slightly sharp roll-off behaviour in comparison to that of Fig. 2a. Considering other upstream stations as a reference station for the cross-correlation analysis same variations in cross-correlation

values are observed at each lag. Moreover, The cross-correlation analyses with reference to the Tarbela station along the downstream of Indus River is not significantly shows of their linear roll-off.

2.2 Nonlinear Analysis of TDF

To explore any possible nonlinearity inherited in the river flow propagation along the Indus River, this paper assesses the MI behaviour of three reference stations and with their upstream stations. The MI values are normalized for each of the three sets with their appropriate reference station's MI value at lag = 0 (Shannon entropy or mutual information at lag = 0). These MI values are now called normalized average of cross

Table 1. Cross-correlation value from Kotri stations with itself and with all its upstream station's along Indus River at different lag values (lag = -4 to 4). The track of the LR curve (Figs. 1b & 2) represent as bold values

Distance from Kotri (km)	From lower to upstream	CC values at different lag = -4 to 4, Along the Indus river from Kotri station								
		-4	-3	-2	-1	0	1	2	3	4
0	Kotri	0.3040	0.4794	0.6797	0.8768	1.0000	0.8768	0.6797	0.4794	0.3040
479.57	Sukkur	0.4160	0.5942	0.7706	0.9227	0.8771	0.6796	0.4853	0.3199	0.1836
690.39	Guddu	0.4595	0.6303	0.7948	0.9202	0.8425	0.6536	0.4697	0.3134	0.1816
991.33	Taunsa	0.6037	0.7199	0.8065	0.8206	0.6954	0.5274	0.3740	0.2374	0.1158
1235.94	Chashma	0.6145	0.7087	0.7774	0.7700	0.6417	0.4904	0.3530	0.2237	0.1091
1334.11	Kalabagh	0.5915	0.6807	0.7496	0.7448	0.6272	0.4838	0.3530	0.2265	0.1128
1535.27	Tarbela	0.5525	0.6544	0.7314	0.7274	0.6160	0.4882	0.3732	0.2568	0.1484

mutual information. The space-time MI value curves are obtained in a way similar to that used in obtaining space-time cross-correlation value curves as discussed in section 1

Using TDF data series all MI values are calculated from lower three reference stations (Fig. 3) separately, with itself, and with all its upstream station's along the Indus River for lag = 0, to lag = -5. To explore the possibility of propagation of nonlinear information, draw a thick black line start from the maximum MI value at reference station to appropriate maximum MI value at other proceeding upstream station. Because of the decreasing behaviour of this thick line we call it nonlinear information propagation roll-off (NR) curve. In Fig. 3a the NR curve starts from Kotri-Kotri MI maximum value at lag = 0 to the next Kotri-Sukkur MI at lag = 2, where it ends (as there is no further MI maximum value appears afterwards). Fig. 3b shows no proceeding NR curve because the upstream stations have no lagged maximum MI value and all maximum values appear on Sukkur station. Fig. 3c represents the MI propagation starting from Guddu-Guddu MI maximum value at lag = 0 to its next maximum Guddu-Taunsa MI value at lag = 1 where it ends as there is no MI maximum value that appears further. Moreover, it is observed that beyond the lag = -5 the MI value curves undergo no change. The three figures (Figs. 3a-c) indicate that the nonlinear information propagates only from Kotri and Guddu stations and prolong for one station Sukkur at lag = 2 and Taunsa at lag = 1 respectively.

3. A COMPARISON OF LINEAR AND NONLINEAR ANALYSES

The linear information (LR curves; Fig. 2) sustain more lag value as compared to nonlinear method (NR curves; Fig. 3). Thus, it can be concluded that for the ensemble TDF of lower five stations (Kotri, Sukkur, Guddu, Taunsa, and Chashma) effectively explains by the linear method as compared to nonlinear method. However, as there are some indications of nonlinear behaviour (Figs. 3 a & c) so, it can't be completely ignored the existence of nonlinearity in this river flow network. It is a separate topic which consider out of the scope of this study. The Fig. 2a shows that LR curve tracking cross-correlation values are higher at lower stations and gradually roll-off at their corresponding upper stations and completely vanish at Chashma. This means that the TDF of the lower five stations can

be well explained through the linear stochastic modelling. However, the upper three station's (Chashma, Kalabagh, and Tarbela) LR tracking cross-correlation values demonstrate the existing strong relations among them at lag = 0. This means that these three stations TDF's are very well explained by the regression. The validity of nonlinear analyses is only effective from Kotri to Sukkur and from Guddu to Taunsa (Figs. 3 a & c). This informs that the possibility of existence of nonlinearity inherited in the propagation of TDF along the Indus River in lower stations. However, their propagation is restricted to the next station and does not prolong further.

4. CONCLUSION

The time series CC and MI analyses, among river flow of each station of IRS show that the overall dominant mechanisms of the TDF propagation along the network are linear, however, some stations demonstrate the existence of possible nonlinearity in it. So, it can't be completely ignored the existence of nonlinearity in this river flow network. According to the results of these approaches, it is concluded that the lower five stations can be well explained through the linear stochastic and upper three stations are very well explained by the regression modelling. The CC and MI analyses not only provide the information about the river flows variation along the network, but, also inform about the geomorphological structure of the river flow network. These analyses also provide the viability to study the behaviour of regional as well as global climatic parameters related to the kind of information propagated and their impact. The possible causes of the existence of nonlinearity are very much discussed in [20] by imposing the temperature and rainfall variability in the simulated river flow network. The result of this paper may help to understand the hydroclimatic study of any river flow network, and make some good contribution in the field of hydrology.

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COMPETING INTERESTS

Authors have declared that no competing interests exist.

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